

SOLVING LOG EQUATIONS DAY 1

NAME key spr 17

SOLVE.

1. $\log_3 x^{-5} = 10$

$$-5 \log_3 X = 10$$

$$\log_3 X = -2$$

$$3^{-2} = X$$

$$X = \frac{1}{9}$$

2. $3^{n+7} = 44$

$$\log_3 44 = n+7$$

$$3.44452 = n+7$$

$$-3.555 = n$$

3. $8 + \ln -5x = 6$

$$\ln -5x = -2$$

$$e^{-2} = -5x$$

$$\frac{e^{-2}}{-5} = x$$

$$x = -.0271$$

4. $1 + \ln 9p = 2$

$$\ln 9p = 1$$

$$e^1 = 9p$$

$$\frac{e^1}{9} = p$$

$$p = .302$$

5. $7 \log_4(x+2) = 0$

$$\log_4(x+2) = 0$$

$$4^0 = x+2$$

$$1 = x+2$$

$$x = -1$$

6. $e^{6x} - 5 = 10$

$$e^{6x} = 15$$

$$\ln 15 = 6x$$

$$\frac{\ln 15}{6} = x$$

$$x = .45134$$

7. $5(2)^{n+9} = 92$

$$2^{n+9} = 92/5$$

$$\log_2 \frac{92}{5} = n+9$$

$$4.2016 = n+9$$

$$n = -4.798$$

8. $\log_7 -5k - 7 = -4$

$$\log_7 -5k = 3$$

$$7^3 = -5k$$

$$343 = -5k$$

$$k = -68.6$$

9. $e^{x-8} - 6 = 87.6$

$$e^{x-8} = 93.6$$

$$\ln 93.6 = x-8$$

$$4.53903 = x-8$$

$$x = 12.53903$$

$$10. \log_4(-19n+1) = \log_4(n^2+91)$$

$$-19n+1 = n^2+91$$

$$0 = n^2+19n+90$$

$$0 = (n+10)(n+9)$$

$$n = -10 \quad n = -9$$

$$11. \log_3 \sqrt[3]{(9x-8)^2} = \frac{4}{3}$$

$$\log(9x-8)^{2/3} = 4/3$$

$$(10^{4/3})^3 = (9x-8)^{2/3 \cdot 3}$$

$$\sqrt[3]{10^4} = \sqrt[3]{(9x-8)^2}$$

$$10^2 = 9x-8$$

$$100 = 9x-8$$

$$108 = 9x$$

$$x = 12$$

*12
won't
work

$$12. 3^{2x+3} = 4^{x-2}$$

$$\log_3 4^{x-2} = 2x+3$$

$$(x-2) \log_3 4 = 2x+3$$

$$(x-2)(1.2619) = 2x+3$$

$$1.2619x - 2.5238 = 2x+3$$

$$-5.5238 = .7381x$$

$$x = -7.4895$$

$$13. 4^{x+1} = 5^{2x-3}$$

$$\log_4 5^{2x-3} = x+1$$

$$(x-3) \log_4 5 = x+1$$

$$(x-3)(1.16096) = x+1$$

$$3.2192x - 3.48288 = x+1$$

$$.32192x = 4.48288$$

$$x = 3.3912$$

$$14. \log_3(x^2-5)^4 = 4$$

$$4 \log_3(x^2-5) = 4$$

$$\log_3(x^2-5) = 1$$

$$3^1 = x^2-5$$

$$8 = x^2$$

$$x = \pm 2.828$$

$$15. 5e^{3x+1} - 3 = 10$$

$$5e^{3x+1} = 13$$

$$e^{3x+1} = 13/5$$

$$\ln 13/5 = 3x+1$$

$$.955511 = 3x+1$$

$$-.044489 = 3x$$

$$x = -.0148$$

$$16. \log(\sqrt[4]{10-5x})^3 = 3$$

$$3 \log(10-5x)^{1/4} = 3$$

$$\log(10-5x)^{1/4} = 1$$

$$(10^1)^4 = (10-5x)^{1/4 \cdot 4}$$

$$10,000 = 10-5x$$

$$9990 = -5x$$

$$x = -1998$$

$$17. \left(\frac{1}{16}\right)^{x-1} = 4^{3x+3}$$

$$(4^{-2})^{x-1} = 4^{3x+3}$$

$$-2x+2 = 3x+3$$

$$-1 = 5x$$

$$x = -1/5$$

$$18. \log(n^2+2n) = \log(81+2n)$$

$$n^2+2n = 81+2n$$

$$n^2 = 81$$

$$n = \pm 9$$