

#113 - Margin of Error Key

- ① sample = 550
64% spent over \$25

$$MOE = 1.96 \sqrt{\frac{.64(.36)}{550}}$$

$$MOE = .0401$$

interval: $.64 \pm .0401$

$$.5999 - .6801$$

or
about

$$60\% - 68\%$$

- ③ 1000 adults
832 supported

$$\frac{832}{1000} = .832$$

$$MOE = 1.96 \sqrt{\frac{.832(.168)}{1000}}$$

$$MOE = .0232$$

interval: $.832 \pm .0232$

$$.8088 - .8552$$

or
about 81% - 86%

- ② 18/225 were damaged

$$\frac{18}{225} = .08 \text{ so } 8\% \text{ are damaged}$$

$$MOE = 1.96 \sqrt{\frac{.08(.92)}{225}}$$

$$MOE = .0354$$

interval: $.08 \pm .0354$

$$.0446 - .1154$$

or about 4½% - 11½%

- ④ 50 products
16% are defective

$$MOE = 1.96 \sqrt{\frac{.16(.84)}{50}}$$

$$MOE = .1016$$

interval: $.16 \pm .1016$

$$.0584 - .2616$$

or about 6% - 26%

90 teens
20%

$$MOE = 1.96 \sqrt{\frac{.20(.80)}{90}}$$

$$MOE = .0826$$

9000 teens
20%

$$MOE = 1.96 \sqrt{\frac{.20(.80)}{9000}}$$

$$MOE = .00826$$

90,000 teens
20%

$$MOE = 1.96 \sqrt{\frac{.20(.80)}{90000}}$$

$$MOE = .0026$$

8) The bigger the sample size, the smaller the MOE!

9) To cut MOE in half, you need to QUADRUPLE the sample size! Here's why:

$$\frac{1}{2} MOE = \frac{1}{2} \cdot 1.96 \cdot \frac{s}{\sqrt{n}}$$

$$\frac{1}{2} MOE = 1.96 \cdot \frac{s}{2\sqrt{n}}$$

$$\frac{1}{2} MOE = 1.96 \frac{s}{\sqrt{4n}}$$

notice that n is being multiplied by 4!

11) Start by finding \bar{x} & s_x

in your calc.... look at the directions in the notes!!

$$\bar{x} = 61.8$$

$$s_x = 4.8$$

$$MOE = 1.96 \frac{4.8}{\sqrt{24}}$$

$$MOE = 1.92$$

$$\text{interval: } 59.88 - 63.72$$

12) 50 bolts
 $\bar{x} = 5.11 \text{ mm}$
 $s_x = 0.1 \text{ mm}$

$$MOE = 1.96 \sqrt{\frac{0.1}{50}}$$

$$MOE = .0277$$

$$\text{interval: } 5.0823 - 5.1377$$

13) 31 grades

$$\bar{x} = 105.84$$

$$s_x = 14.27$$

$$MOE = 1.96 \frac{14.27}{\sqrt{31}}$$

$$MOE = 5.0234$$

$$\text{interval: } 9.2466 - 19.2934$$

$$\text{MOE} = 1.96 \frac{14.27}{\sqrt{90}}$$

$$\textcircled{15} \text{ MOE} = 1.96 \frac{14.27}{\sqrt{250}}$$

$$\text{MOE} = 2.9482$$

$$\text{MOE} = 1.7689$$

The margin of error went down! Almost cut in half!

Now its even lower!

$\textcircled{16}$ The bigger the sample, the lower the MOE!

$\textcircled{17}$ a) 750 adults
14% lat hours

$$\textcircled{b} .14 \pm .0248$$

$$.1152 - .1648$$

so about $11\frac{1}{2}\% - 16\frac{1}{2}\%$

$$\text{MOE} = 1.96 \sqrt{\frac{.14(.86)}{750}}$$

$$\text{MOE} = .0248$$

\textcircled{c} I would say that this statistic isn't true! Our statistic was 14% and with the MOE it should only reach as high as $16\frac{1}{2}\%$

$\textcircled{18}$ a) Do this in your calc!

$$\bar{x} = 31.58$$

$$s_x = .3259$$

$$\textcircled{b} \text{ MOE} = 1.96 \frac{.3259}{\sqrt{10}}$$

$$\text{MOE} = .20199$$

$$\textcircled{c} 31.58 \pm .20199$$

$$31.37801 - 31.78199$$

\textcircled{d} Julie does have a reason to complain! 31.8 is slightly higher than the high end of the interval.

$\textcircled{19}$ 5% of voters

$$\text{MOE} \pm 5\%$$

Not yet! The MOE gives an interval of 46-56% of votes. He could lose the election!!