

AFM HW 6 - EXPONENTIAL GROWTH AND DECAY

NAME key

1. Convert the following percentages into a growth or decay factor (common ratio)

-12.5%

$$.875$$

+ 1%

$$1.01$$

+ 4.3%

$$1.043$$

^{1-.76}
- 76%

$$.24$$

+ 33%

$$1.33$$

- 2.6%

$$.974$$

2. Annual sales for a fast food restaurant are \$650,000 and are increasing at a rate of 4% each year. Write an exponential function to model the sales.

$$y = 650,000(1.04)^x$$

a) What are the sales after 7 years?

$$650,000(1.04)^7$$

$$\$855,355.66$$

b) After how many years will the sales be \$1,000,000?

$$1,000,000 = 650,000(1.04)^x$$

$$\frac{20}{13} = 1.04^x$$

$$\log_{1.04} \frac{20}{13} = x$$

$$x = 10.984$$

~ 11 yrs

3. The population of a town is 2500 people and is decreasing at a rate of 3.5% each year. Write an exponential function to model the population.

$$y = 2500(.965)^x$$

a) What is the population of town after 5 years?

$$2500(.965)^5$$

$$= 2092.07$$

~ 2092 people

b) When will only half the population be left?

$$1250 = 2500(.965)^x$$

$$\frac{1}{2} = .965^x$$

$$\log_{.965} \frac{1}{2} = x$$

$$x = 19.4556$$

~ 19½ yrs

4. The population of a school is 800 students and is increasing at a rate of 2% each year. Write an exponential function to model the population.

$$y = 800(1.02)^x$$

a) What is the population of the school after 9 years?

$$800(1.02)^9$$

$$= 956.07$$

~ 956 students

b) When will the school double in size?

$$1600 = 800(1.02)^x$$

$$2 = 1.02^x$$

$$\log_{1.02} 2 = x$$

$$x = 35 \text{ yrs}$$

5. In 1991 Mr. Davis purchased his home for \$160,000. Since then, the value of the home has increased about 5% each year. Write an exponential function to model the value of the home.

$$y = 160,000(1.05)^x$$

a) What is the value of Mr. Davis's home today?

$$2016 - 1991 \rightarrow 25 \text{ yrs}$$

$$160,000(1.05)^{25}$$

$$\$541,816.79$$

b) When will the house be worth \$750,000?

$$750,000 = 160,000(1.05)^x$$

$$75/16 = 1.05^x$$

$$\log_{1.05} 75/16 = x$$

$$x \sim 31\frac{1}{2} \text{ or } 32 \text{ yrs}$$

6. Find the amount in an account after 15 years if \$5000 was initially invested and the account earns 8% annual interest compounded quarterly.

$$A = 5000(1 + \frac{.08}{4})^{4 \cdot 15}$$

$$A = 5000(1.02)^{60}$$

$$\$16,405.15$$

$$t = 15$$

$$P = 5000$$

$$r = .08$$

$$n = 4$$

7. Find the length of time needed to earn \$124.49 if Megan invests \$957.62 at 6.5% interest, compounded continuously.

$$A = 124.49 + 957.62 = 1082.11$$

$$P = 957.62$$

$$r = .065$$

$$1082.11 = 957.62 e^{.065t}$$

$$1.129999 = e^{.065t}$$

$$\ln 1.129999 = .065t$$

$$t \sim 1.88 \text{ or } 2 \text{ yrs}$$

8. A savings account with interest compounded quarterly increased from \$2500 to \$3033.52 in three years. What annual interest rate did the account earn over this time period?

$$n = 4$$

$$P = 2500$$

$$A = 3033.52$$

$$t = 3$$

$$3033.52 = 2500(1 + \frac{r}{4})^{4 \cdot 3}$$

$$1.2134 = (1 + \frac{r}{4})^{12}$$

$$1.01625 = 1 + \frac{r}{4}$$

$$.01625 = \frac{r}{4}$$

$$.065 = r$$

$$r = 6.5\%$$

9. If Amanda borrows \$3500 from the bank for 6 months at 7 1/2% interest, compounded continuously, how much will she have to pay back?

$$P = 3500$$

$$t = \frac{1}{2}$$

$$r = .075$$

$$A = 3500 e^{.075(\frac{1}{2})}$$

$$A = \$3,633.74$$

10. If Paige invests \$800 in an account for 6 years that compounds monthly and receives \$168 interest, what is her annual interest rate?

$$P = 800$$

$$t = 6$$

$$n = 12$$

$$968 = 800(1 + \frac{r}{12})^{12 \cdot 6}$$

$$1.21 = (1 + \frac{r}{12})^{72}$$

$$1.00265 = 1 + \frac{r}{12}$$

$$.00265 = \frac{r}{12}$$

$$.0318 = r$$

$$r \sim 3.2\%$$

$$A = 800 + 168 = 968$$