

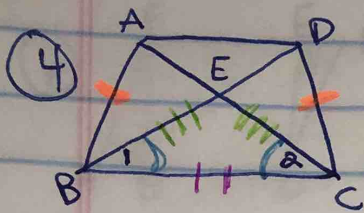
Given: $\angle 1 \cong \angle 2$

$\overline{AE} \cong \overline{CF}$

$\overline{DE} \parallel \overline{FB}$

Prove: ABCD is a parallelogram

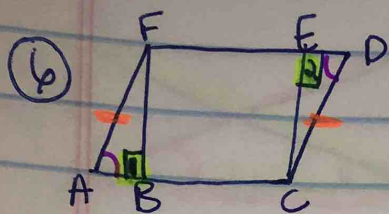
- | | |
|---|--|
| ① $\angle 1 \cong \angle 2$ | ① Given |
| ② $\overline{AB} \parallel \overline{DC}$ | ② If alternate interior angles are $\cong \rightarrow$ lines are \parallel [1] |
| ③ $\overline{AE} \cong \overline{CF}$ | ③ Given |
| ④ $\overline{EF} \cong \overline{EF}$ | ④ Reflexive |
| ⑤ $AE + EF = EF + CF$ | ⑤ Addition [3, 4] |
| ⑥ $AE + EF = AF$
$EF + CF = EC$ | ⑥ Segment Addition |
| ⑦ $AF = EC$ | ⑦ Substitution [5, 6] |
| ⑧ $\overline{DE} \parallel \overline{FB}$ | ⑧ Given |
| ⑨ $\angle 3 \cong \angle 4$ | ⑨ If lines are parallel \rightarrow alt. int. angles are \cong [8] |
| ⑩ $\triangle AFB \cong \triangle CED$ | ⑩ ASA [1, 7, 8] |
| ⑪ $\overline{DC} \cong \overline{AB}$ | ⑪ CPCTC [10] |
| ⑫ ABCD is a parallelogram | ⑫ One set of opposite sides are \parallel & \cong [2, 11] |



Given: $ABCD$ is an isosceles trapezoid with $\overline{AD} \parallel \overline{BC}$

Prove: $\triangle EBC$ is isosceles

- | | |
|---------------------------------------|--|
| ① $ABCD$ is an isosceles trapezoid | ① Given |
| ② $\overline{AB} \cong \overline{DC}$ | ② Def. isosceles trapezoid [1]
(legs are \cong) |
| ③ $\overline{AC} \cong \overline{BD}$ | ③ Def. isosceles trapezoid [1]
(Diagonals are \cong) |
| ④ $\overline{BC} \cong \overline{BC}$ | ④ Reflexive Property |
| ⑤ $\triangle ABC \cong \triangle DCB$ | ⑤ SSS [2, 3, 4] |
| ⑥ $\angle 1 \cong \angle 2$ | ⑥ CPCTC [5] |
| ⑦ $\overline{BE} \cong \overline{EC}$ | ⑦ Isosceles Triangle Theorem [6] |
| ⑧ $\triangle BEC$ is isosceles | ⑧ Def. of Isosceles Triangle [7] |

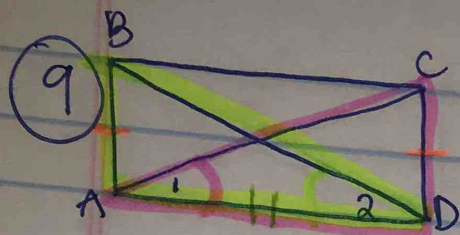


Given ACDF is a parallelogram

$FB \perp AC$, $CE \perp FD$

Prove: $\overline{AB} \cong \overline{BC}$

- | | |
|--|---|
| ① ACDF is a parallelogram | ① Given |
| ② $\overline{AF} \cong \overline{DC}$ | ② Def. of parallelogram
(opp. sides are \cong) [1] |
| ③ $\angle A \cong \angle D$ | ③ Def. of parallelogram
(opp. angles are \cong) [1] |
| ④ $FB \perp AC$, $CE \perp FD$ | ④ Given |
| ⑤ $\angle 1$ is a right angle
$\angle 2$ is a right angle | ⑤ Def. of perpendicular
[4] |
| ⑥ $\angle 1 \cong \angle 2$ | ⑥ Right Angle Theorem [5] |
| ⑦ $\triangle BAF \cong \triangle EDC$ | ⑦ AAS [2, 3, 5] |
| ⑧ $\overline{AB} \cong \overline{BC}$ | ⑧ CPCTC [7] |



Given: ABCD is a rectangle

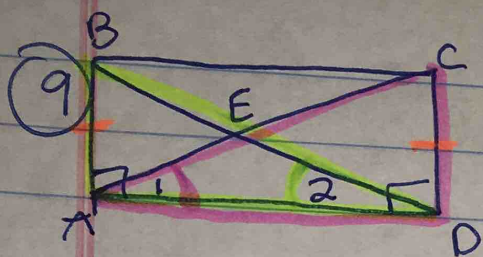
Prove: $\angle 1 \cong \angle 2$

- ① ABCD is a rectangle
- ② $\overline{AB} \cong \overline{CD}$
- ③ $\overline{AC} \cong \overline{DB}$
- ④ $\overline{AD} \cong \overline{AD}$
- ⑤ $\triangle BAD \cong \triangle CDA$
- ⑥ $\angle 1 \cong \angle 2$

- ① Given
- ② Def. of Rectangle
(opp. sides are \cong) [1]
- ③ Def. of Rectangle
(diagonals are \cong) [1]
- ④ Reflexive Property
- ⑤ SSS [2, 3, 4]
- ⑥ CPCTC [5]

*I did this one 2 ways...

see next page ☺



Given: ABCD is a rectangle

Prove: $\angle 1 \cong \angle 2$

- ① ABCD is a rectangle
- ② $\overline{AB} \cong \overline{DC}$
- ③ $\angle BAD$ is a right angle
 $\angle CDA$ is a right angle
- ④ $\angle BAD \cong \angle CDA$
- ⑤ $\overline{AD} \cong \overline{AD}$
- ⑥ $\triangle BAD \cong \triangle CDA$
- ⑦ $\angle 1 \cong \angle 2$

- ① Given
- ② Def. Rectangle [1]
(opp. sides are \cong)
- ③ Def. Rectangle [1]
(all angles are right angles)
- ④ Right Angle Theorem [3]
- ⑤ Reflexive
- ⑥ SAS [2, 4, 5]
- ⑦ CPCTC [6]